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A New Special Right Triangle: $15^\circ \cdot 75^\circ \cdot 90^\circ$

The **.366 | 1.366 | $\sqrt{2}$ Baseline of the Special Right Triangle Series**

$15^\circ \cdot 75^\circ \cdot 90^\circ$

$30^\circ \cdot 60^\circ \cdot 90^\circ$

$45^\circ \cdot 45^\circ \cdot 90^\circ$

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Extract

*In a previous analysis, **Fractal Triangles**, I explored a series of triangles that complement the **basic** and **special** triangles that are presented in textbooks on geometry. In this essay, I will present a baseline triangle that, in my view, has been overlooked throughout the study of geometry. It is my interpretation that for centuries this series of triangles has had an undue emphasis placed upon the basic and special triangles, as though these were in fact the only relevant triangles.*

In a previous analysis of a series of fractal triangles, I illustrated how the fractal triangles are complementary to the traditionally cited basic and special triangles. A summary view of the basic and special triangles presented in textbooks on geometry reads as follows.

The **basic** triangles **3 · 4 · 5** and **5 · 12 · 13** are generally cited in most textbooks on geometry. These triangles are presented as of their side measurements. While the **special** **$45^\circ \cdot 45^\circ \cdot 90^\circ$** and **$30^\circ \cdot 60^\circ \cdot 90^\circ$** triangles are presented as of the measurements of their angles. The reasons for this arbitrary presentation concern an

age-old desire to work with whole numbers. It has been cited that the ancients avoided the decimal expressions of irrational numbers; and this appears to be still the case today. Although treatments of the triangles $1 \cdot 1 \cdot \sqrt{2}$ and $1 \cdot \sqrt{3} \cdot 2$ are common, hardly ever does one find any elementary study related to the triangle $1 \cdot 2 \cdot \sqrt{5}$. Again, this may have to do with the fractional expression of its angles. The angles of the $1 \cdot 2 \cdot \sqrt{5}$ triangle are: $26.5651^\circ \cdot 63.4349^\circ \cdot 90^\circ$. Small wonder this triangle is referred to by its side measurements albeit symbolically by the square root of 5. $1 \cdot 2 \cdot \sqrt{5}$ which translate into the side measurements of $1 \cdot 2 \cdot 2.236067978$.

The two different series of right triangles, along with a fractal triangle, then, may be summarized in the following manner:

	Side	Symbolic	
	<u>Measurements</u>	<u>Notation</u>	<u>Angles</u>
Special:	$1 \cdot 1 \cdot 1.4142$	$1 \cdot 1 \cdot \sqrt{2}$	$45^\circ \cdot 45^\circ \cdot 90^\circ$
Special:	$1 \cdot 1.732 \cdot 2$	$1 \cdot \sqrt{3} \cdot 2$	$30^\circ \cdot 60^\circ \cdot 90^\circ$
<i>Fractal</i>	$1 \cdot 2 \cdot 2.236$	$1 \cdot 2 \cdot \sqrt{5}$	$26.5651^\circ \cdot 63.4349^\circ \cdot 90^\circ$
Basic:	$3 \cdot 4 \cdot 5$	$3 \cdot 4 \cdot 5$	$36.8699^\circ \cdot 53.1301^\circ \cdot 90^\circ$
Basic:	$5 \cdot 12 \cdot 13$	$5 \cdot 12 \cdot 13$	$22.6199^\circ \cdot 67.3801^\circ \cdot 90^\circ$

As I gaze upon this particular placement of the different triangle series, one element stands out: the logic of considering a triangle of $15^\circ \cdot 75^\circ \cdot 90^\circ$. In other words, logic would tell us that one might consider a series of triangles as of increments/decrements of fifteen degrees:

$45^\circ \cdot 45^\circ \cdot 90^\circ$

$30^\circ \cdot 60^\circ \cdot 90^\circ$

$15^\circ \cdot 75^\circ \cdot 90^\circ$

One can only wonder why the series of special triangles has not been presented in its obvious progression, and only two of the triangles within the series have been emphasized in textbooks on geometry over the centuries. In order to understand the possible significance of considering the **15° · 75° · 90° special** triangle, along with its corresponding series, a few comments are in order regarding the Earth/matrix temperature scale.

For the past few years, I have been presenting the idea of utilizing a thermodynamic temperature scale that has the boiling point of water (**BPW**) as unit one (1.0) and/or the freezing point of water (**FPW**) as unit one (1.0). Variations of these scales have been presented in the Earth/matrix series of essays, but I will concentrate on the scale that employs the freezing point of water as unit one in this essay. If one assigns the freezing point of water as unit one (1.0), then the boiling point of water will be registered as 1.3661 on that same scale, where absolute zero is precisely 0.00. The difference, then, between the freezing point of water (1.0) and the boiling point of water (1.3661) is represented in the value of .3661 on the Earth/matrix thermodynamic temperature scale.

I have also shown how the values in relation to the boiling/freezing points of water are related to the square root of three (1.732050808).

$$1.3661 \times 1.732050808 \text{ equals } 2.366154609$$

The significant point is that the 2.3661, in fact, represents the sum of the values for the freezing and boiling points of water on the scale:

$$1.0 \text{ plus } 1.3661 = 2.3661$$

These points are treated in much more detail in the essays and book that I have written about the Earth/matrix thermodynamic temperature scales.

On the Kelvin scale the corresponding values are distinct:

$$\text{Boiling point of water} = 373.15 \text{ k}$$

$$\text{Freezing point of water} = 273.15 \text{ k}$$

$$373.15 / 273.15 = 1.366099213 \text{ (1.3661 rounded off).}$$

$$373.15 \text{ times the square root of three equals } 646.2281563$$

$$273.15 \text{ plus } 373.15 = 646.3$$

1.0 freezing point of water

.3661 *difference* between boiling/freezing points of water

One cannot expect to consider that the obvious correspondence between the side values of the special right triangle and the values relating to the boiling/freezing points of water can be the result of happenstance. Obviously the relationship obeys the properties and characteristics of matter-energy. It remains to discuss fully what these properties and characteristics may be in this regard. For now, we simply make the point of comparison.

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